

# **Buckling of composite plates in hygrothermal conditions**

**A thesis submitted in partial fulfillment for requirements of degree in  
*Bachelor of technology***

***In***

***Civil engineering***

***By***

***Deepak Kumar Samal***

***Roll No:10601028***

**Under The Guidance of  
Prof. S. K. Sahu**



**Department of Civil Engineering  
National Institute of Technology Rourkela  
Rourkela-769008,  
Orissa, India**

***May 2010***

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**INDIA**

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## ***CERTIFICATE***

*This is to certify that the thesis entitled “**Buckling of Composite Plates in Hygrothermal Conditions**” submitted by **Mr. Deepak Kumar Samal** in partial fulfillment of requirement of **Btech Degree in Civil Engineering** at the **NATIONAL INSTITUTE OF TECHNOLOGY, ROURKELA** (Deemed University) is an authentic work carried out by him under my supervision and guidance.*

*To the best of my knowledge the matter embodied in the thesis has not been submitted to any other University/Institute for the award of any degree or diploma.*

*Date:*

***Prof. S.K. Sahu***

*Place:*

***Dept of Civil Engineering***

***National Institute of Technology***

***Rourkela-769008***

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**Deepak Kumar Samal**

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## **ABSTRACT**

*This paper deals with the analysis of buckling effects of composites in an hygrothermal environment. It is found from the analysis of various researchers world over that the effect of temperature and moisture which the composite materials are generally subjected to in case of space crafts and all have a considerable effect on the critical load carrying capacity of the composite plates which decreases linearly with uniform increase in moisture content and non-linearly with increase in temperature. The objective is to check the consistency of above results using different set of material properties of composites and further it within the scope of available resources.*

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# **Chapter-1**

## **Introduction**

## **Introduction**

*Composites are materials consisting of two or more different substances which differ in their properties and are insoluble in each other but as a combination gives rise to a new form of improved material characteristics.*

*Composites consists therefore of various phases. They may be two phase, three phase or so on. But we are mainly dealing with two phase composites. The two phase composites is broadly divided into two types. They are mainly particulate composites or fibre reinforced composites. The particulate composites are those in which the particles are dispersed in a matrix in a random fashion. Hence they may be a non metal dispersed in a non metallic matrix( mica flakes reinforced with glass), a metal dispersed in a non metal matrix(aluminium particles in polyurethane rubber), a metal particle dispersed in a metal matrix(lead particles in copper alloys) or a non metal dispersed in a metallic matrix(silicon carbide particles in aluminium).*

*Fibre reinforced composites are the one we deal with mostly for all the analysis. They may be of polymer matrix composites(E glass fibre with Epoxy matrix), metal matrix composites(boron fibre in aluminium matrix), ceramic matrix composites(silicon carbide fibres in silicon fibre matrix) or carbon/carbon composites(carbon fibre in carbon matrix).*

*The popularity of composite materials has been due to their better material properties which is absent in case of normal isotropic materials. The properties exhibited by the composite materials which has been instrumental in their wide popularity and high usability are its greater specific modulus, higher specific strength , better impact resistance, better damping of vibrations, high stiffness, corrosion resistant, light weight, low maintenance costs etc . Hence their applicability is numerous in the fields like electrical application , welding machine parts, automotive field to produce racing cars and all, in sporting goods for production of tennis rackets or snow skis, aircrafts or space crafts, marine field and so on.*

## **Review of Literature**

*Limited research has been done to characterize the hygrothermal buckling response of the structures made of composites. However, much of the published works on hygrothermal buckling is based on deterministic analysis, notable among them are Whitney and Ashton(1971) , Lee and Yen(1989) , Ram and Sinha(1992) , Flaggs et al.(1978) , Parhi and Ram and Sinha(2001) . Nakagiri et al.(1990) have studied all edges simply supported by a laminated plate with the stochastic finite element method taking fiber orientation, layer thickness and number of*

layers as random variables, and found that the overall stiffness of FRPs laminated plates is largely dependent on the fiber orientation.

Singh et al. (2001) have presented the buckling of composite cylindrical panels with uncertain material properties using the higher shear deformation theory (HSDT) based finite element method (FEM) with the first order perturbation technique (FOPT).

Englested and Reddy(1994) studied metal matrix composites based on probabilistic micro mechanics nonlinear analysis. They used Monte Carlo Simulation (MCS) with different probabilistic distributions to incorporate the uncertainty in basic material properties.

Chen et al.(1992) have presented a probabilistic method to evaluate the effect of uncertainties in geometrical and material properties of structure on the random vibration response.

Yadav and Verma(1997) studied the buckling response of thin cylindrical shells with random material properties using classical laminate theory and employed the FOPT for obtaining the second order statistics of the buckling loads.

Graham and Siragy(2001) have studied the variability of the random buckling loads of beams and plates with stochastically varying material and geometric properties using the concept of the variability response function.

Singh et al.(2001) have studied the effect of randomness in material properties on the free vibration and buckling analysis of the composite plate.

### **Aim and scope of Present Study:**

To analyse the effect of buckling experimentally on composite plates in hygrothermal conditions, that is in conditions of application of temperature and moisture experimentally and validate the result with theoretical values.

# *Chapter-2*

## *Experimental Study*

## ***Present developments:***

### **For aluminium plates**

The buckling loads of different isotropic aluminium plates were first studied experimentally using fixed end supports using a Universal Testing Machine.

### ***SPECIFICATION OF THE ALUMINIUM PLATES:***

TABLE-1(Specification of Aluminium Plates)

| <b><i>SAMPLE</i></b> | <b><i>Lu</i></b> | <b><i>BREADTH</i></b> | <b><i>THICKNESS</i></b> | <b><i>WEIGHT</i></b> |
|----------------------|------------------|-----------------------|-------------------------|----------------------|
| <i>A</i>             | <i>163mm</i>     | <i>122mm</i>          | <i>2mm</i>              | <i>100gm</i>         |
| <i>B</i>             | <i>155mm</i>     | <i>119mm</i>          | <i>2mm</i>              | <i>97gm</i>          |
| <i>C</i>             | <i>168mm</i>     | <i>116mm</i>          | <i>2mm</i>              | <i>101gm</i>         |

### **For composite plates**

#### ***FABRICATION OF COMPOSITE PLATES***

The composite plates were fabricated in the laboratory using glass fibre epoxy and hardener. Other accessories like hand cuffs, sprayer, roller, weighing machine and scissors were used.

Six different plates were fabricated the details of which are tabulated below.

Table-2(Specification of composite plates)

| <b><u>SPECIMEN</u></b> | <b><u>WEIGHT(gm)</u></b> | <b><u>WT. OF EPOXY(gm)</u></b> | <b><u>WT. OF HARDENER(gm)</u></b> |
|------------------------|--------------------------|--------------------------------|-----------------------------------|
| <i>1</i>               | <i>364</i>               | <i>300</i>                     | <i>24</i>                         |
| <i>2</i>               | <i>366</i>               | <i>300</i>                     | <i>24</i>                         |
| <i>3</i>               | <i>410</i>               | <i>273</i>                     | <i>22</i>                         |
| <i>4</i>               | <i>358</i>               | <i>240</i>                     | <i>20</i>                         |
| <i>5</i>               | <i>356</i>               | <i>192</i>                     | <i>16</i>                         |
| <i>6</i>               | <i>404</i>               | <i>220</i>                     | <i>18</i>                         |

The plates were then cut using a cutter mainly of square dimensions and further test are to be carried out.



*fig-1(a):before buckling*



*fig-1(b):after buckling*

*N.B:All through the experiment the support condition was taken to be fixed at both ends*

# *Chapter-3*

*Results and discussions*

## **GENERAL THEORITICAL FORMULA FOR BUCKLING WHEN BOTH ENDS ARE FIXED:**

$$P_{cr} = (4*(3.141)^2*EI)/(Lu^2)$$

Where  $P_{cr}$ =critical load

$E$ =modulus of elasticity of aluminium=69 GPa

$I$ =least moment of inertia of plate about a axis

$Lu$ =unsupported length of the plate

The buckling load is found by drawing tangent from the pre and post buckling stage of a load displacement graph.

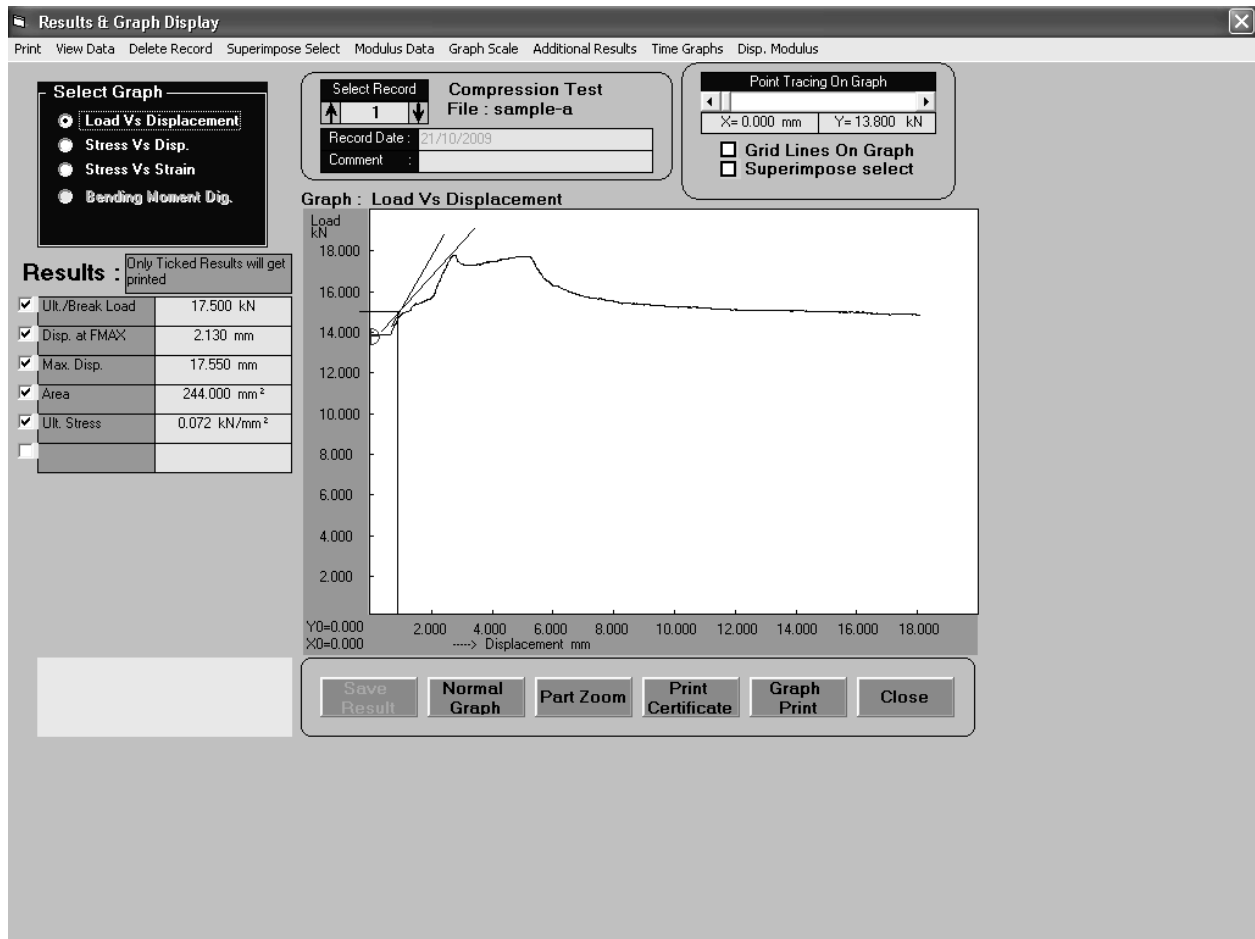
### **For aluminium plates**

Table-3(ultimate load carrying capacity)

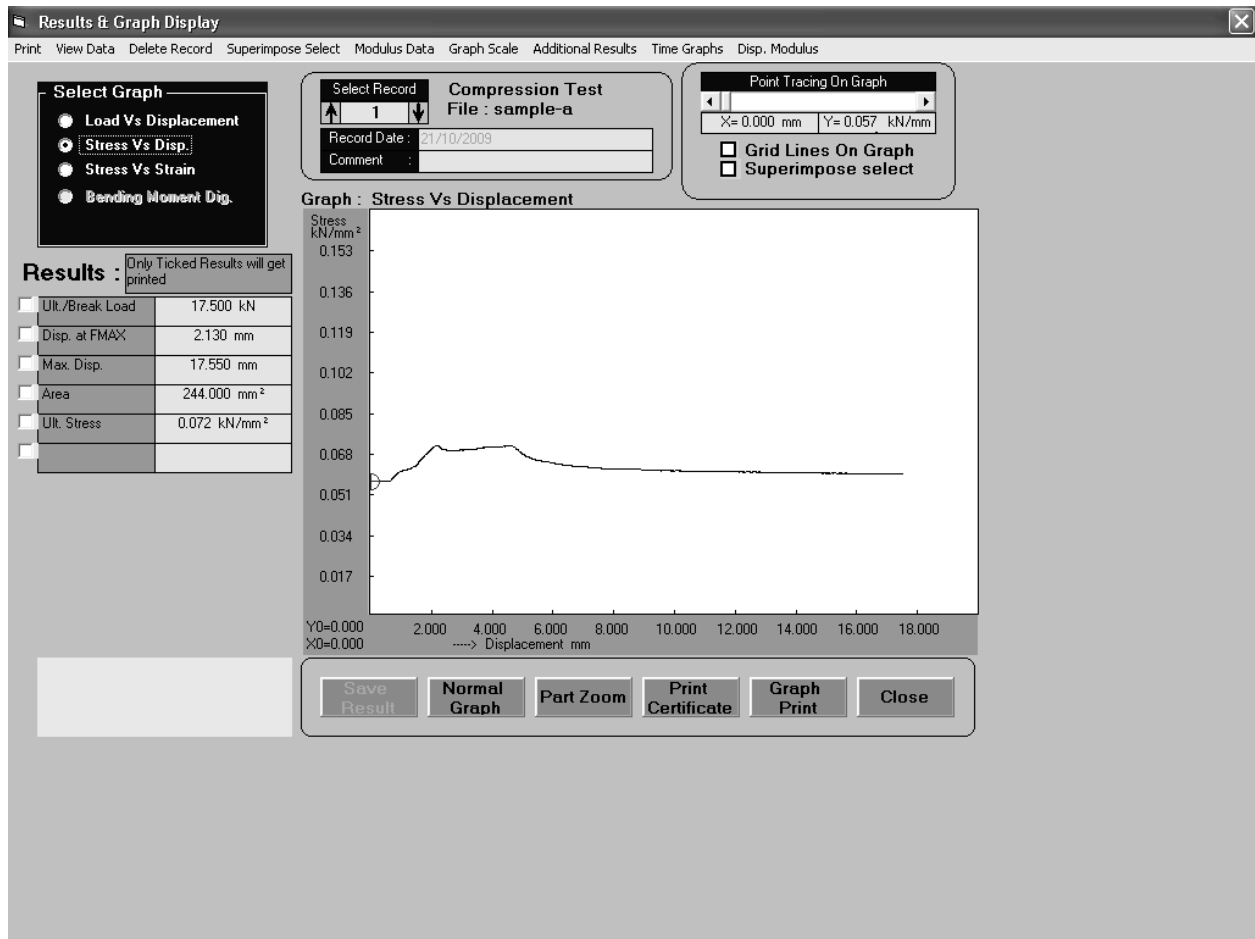
| <b>Sample</b> | <b>Ultimate load(kn)</b> |
|---------------|--------------------------|
| <i>A</i>      | <i>17.5</i>              |
| <i>B</i>      | <i>16</i>                |
| <i>C</i>      | <i>16.45</i>             |

### **Sample graphs**

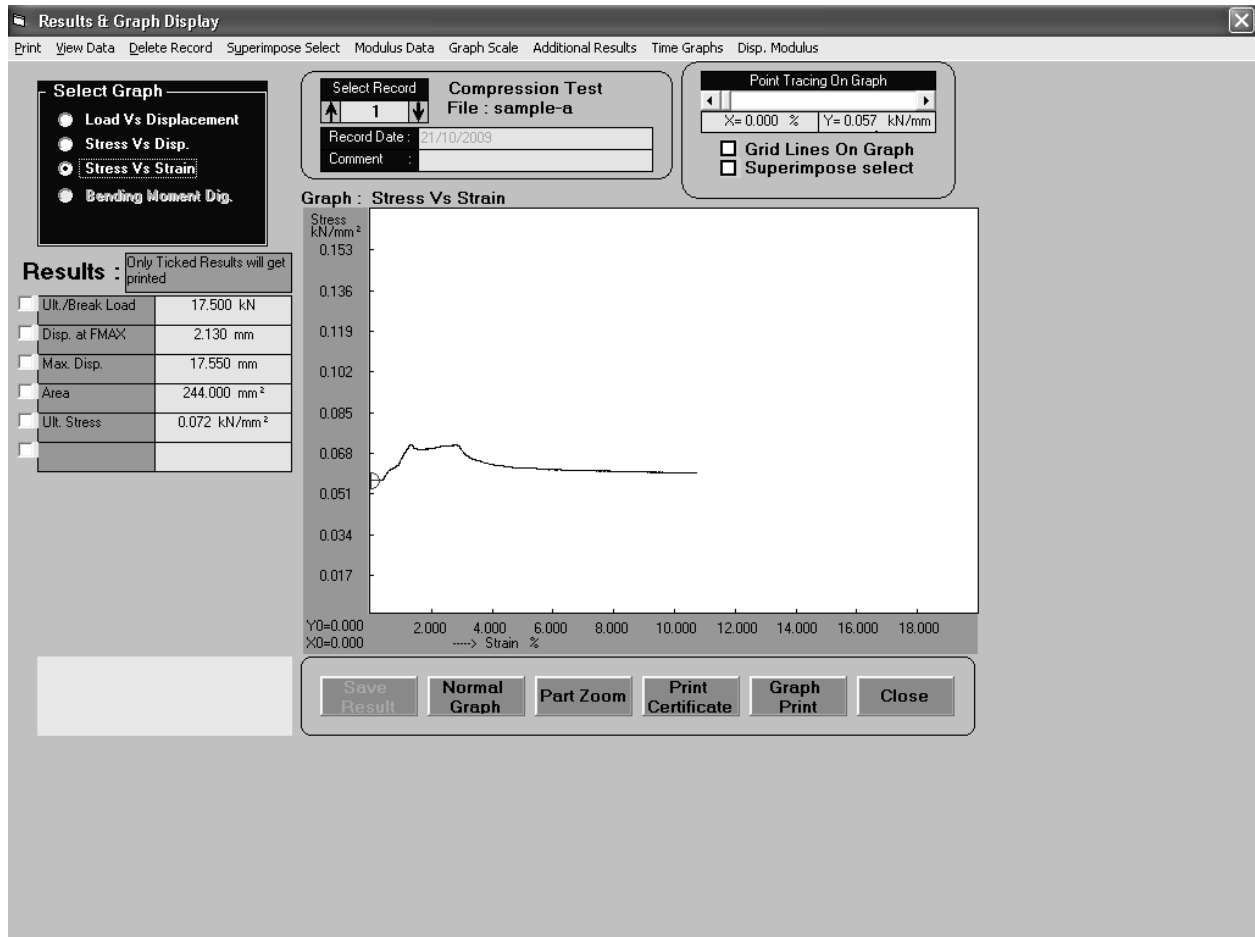




Graph-1(load vs displ of aluminium plate-sampleA)



*graph-2(stress vs displacement)*



Graph-3(stress vs strain)

***For composite plates***

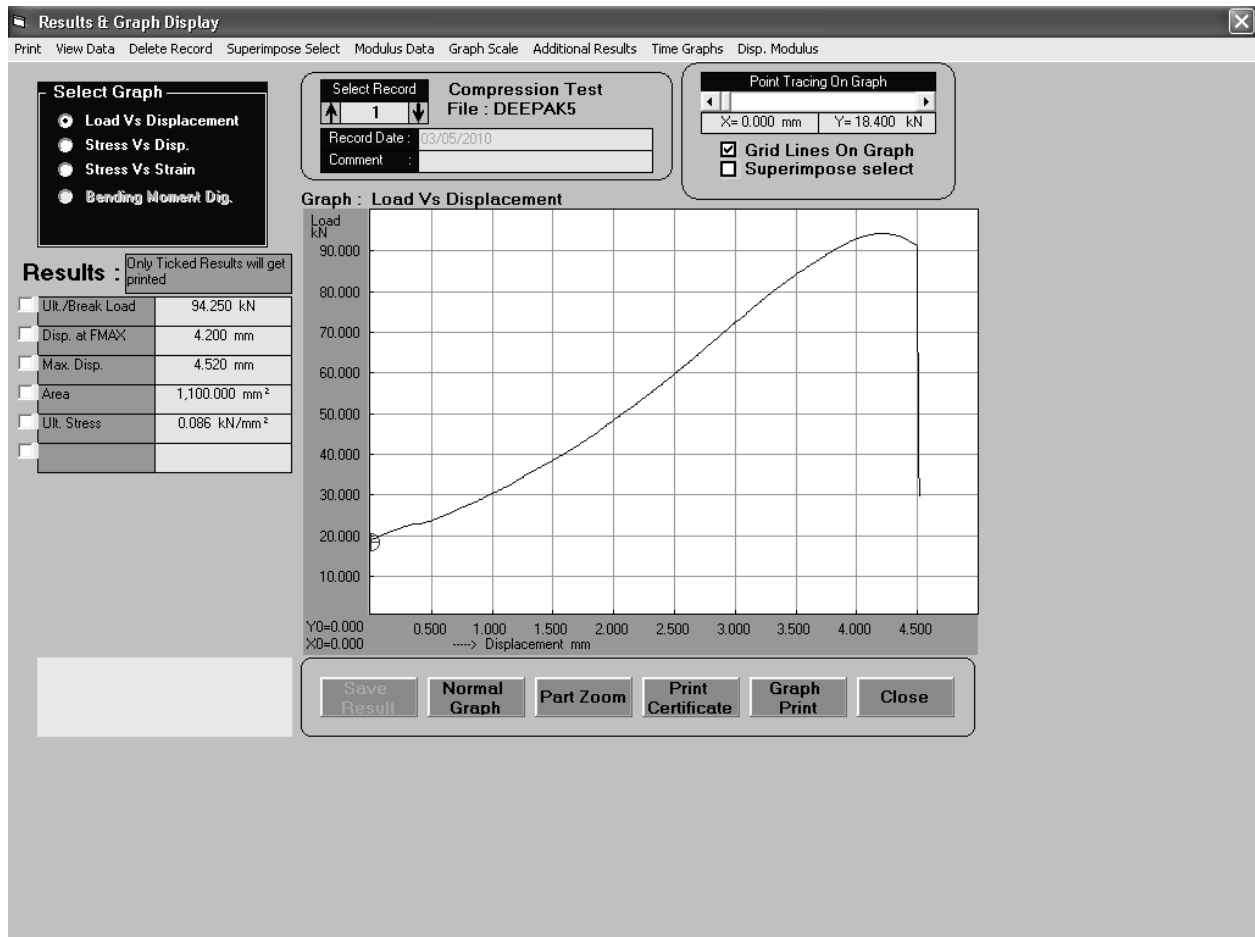
***(list of specimen used and their specifications)***

*Table-4(Specification of composite plates after moisture treatment and the ultimate load carrying capacity)*

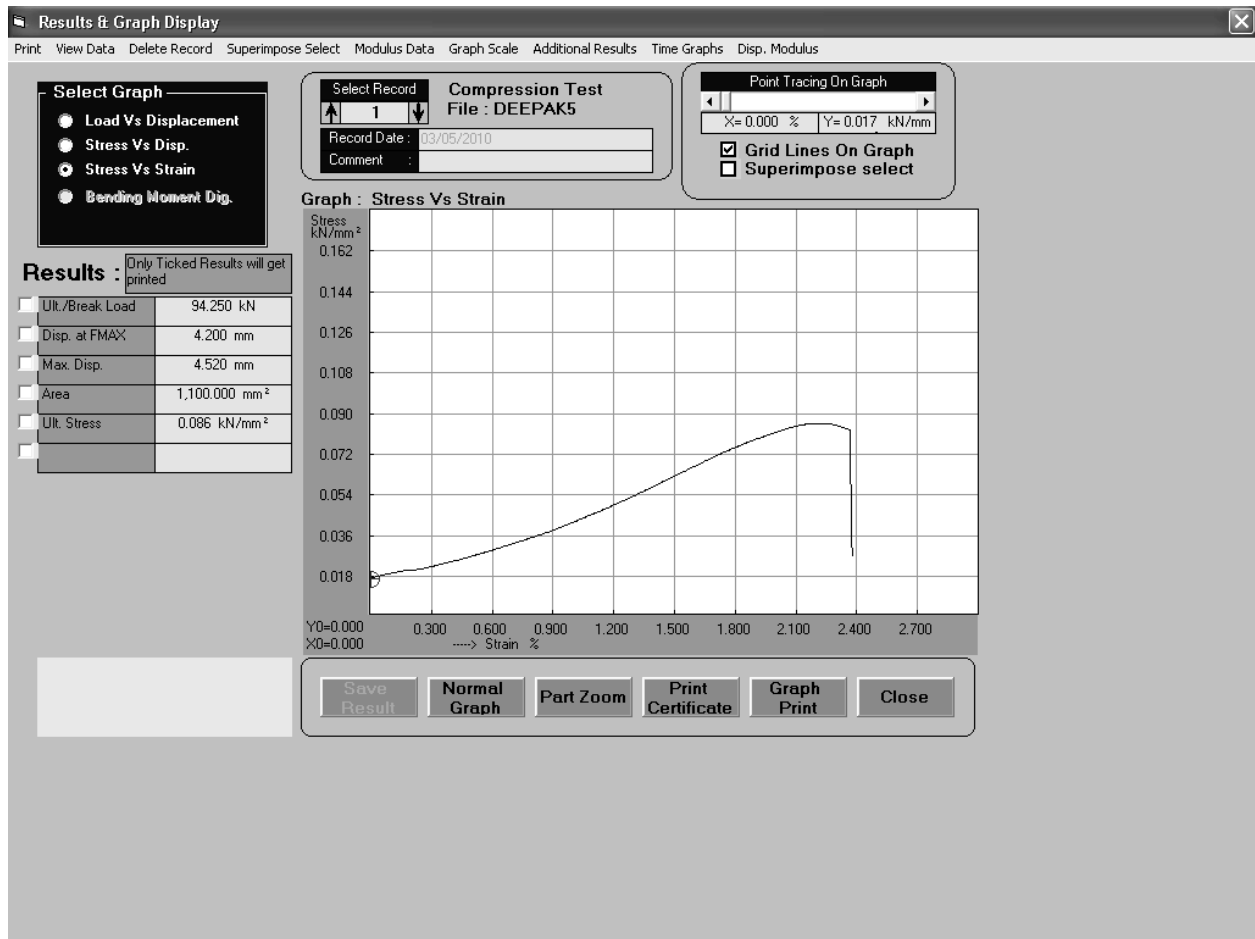
| <b><i>Specimen</i></b> | <b><i>Size(cm)</i></b> | <b><i>Thickness(cm)</i></b> | <b><i>Moisture</i></b> | <b><i>Ultimate load</i></b> |
|------------------------|------------------------|-----------------------------|------------------------|-----------------------------|
| <i>1</i>               | <i>24*24</i>           | <i>0.6</i>                  | <i>75%</i>             | <i>78.3kn</i>               |
| <i>2</i>               | <i>22*22</i>           | <i>0.6</i>                  | <i>60%</i>             | <i>57.7kn</i>               |
| <i>5</i>               | <i>20*20</i>           | <i>0.6</i>                  | <i>75%</i>             | <i>94.25kn</i>              |
| <i>6</i>               | <i>21*21</i>           | <i>0.6</i>                  | <i>60%</i>             | <i>66.3kn</i>               |

*Generally the effect of temperature and moisture has a deteriorating effect on the composite plates by bringing down its strength and stiffness characteristics. The effect of temperature generally causes a softening of the fibres and the effect of moisture causes plasticization due to absorbed moisture. This is evident from the results obtained.*

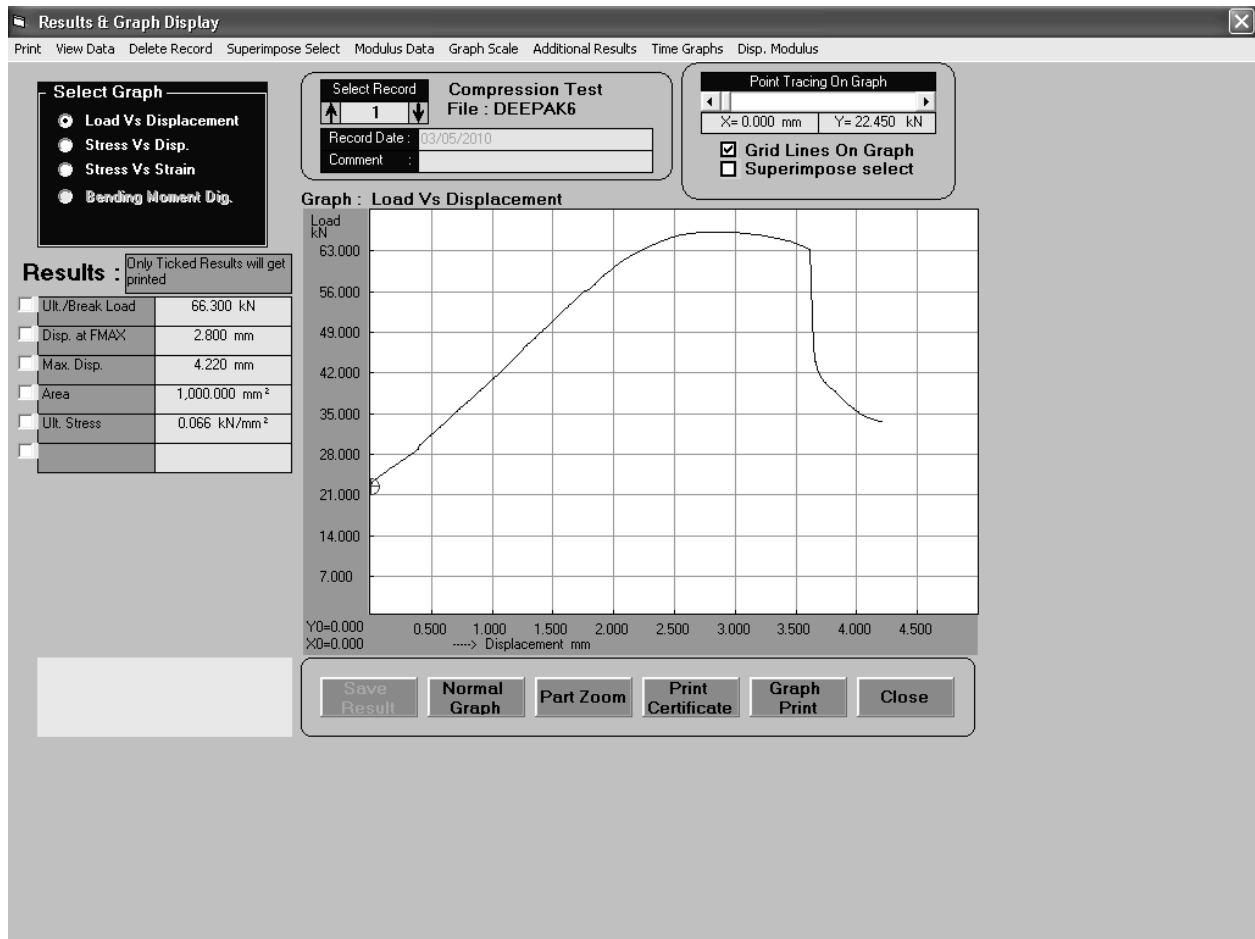
## Sample Graphs



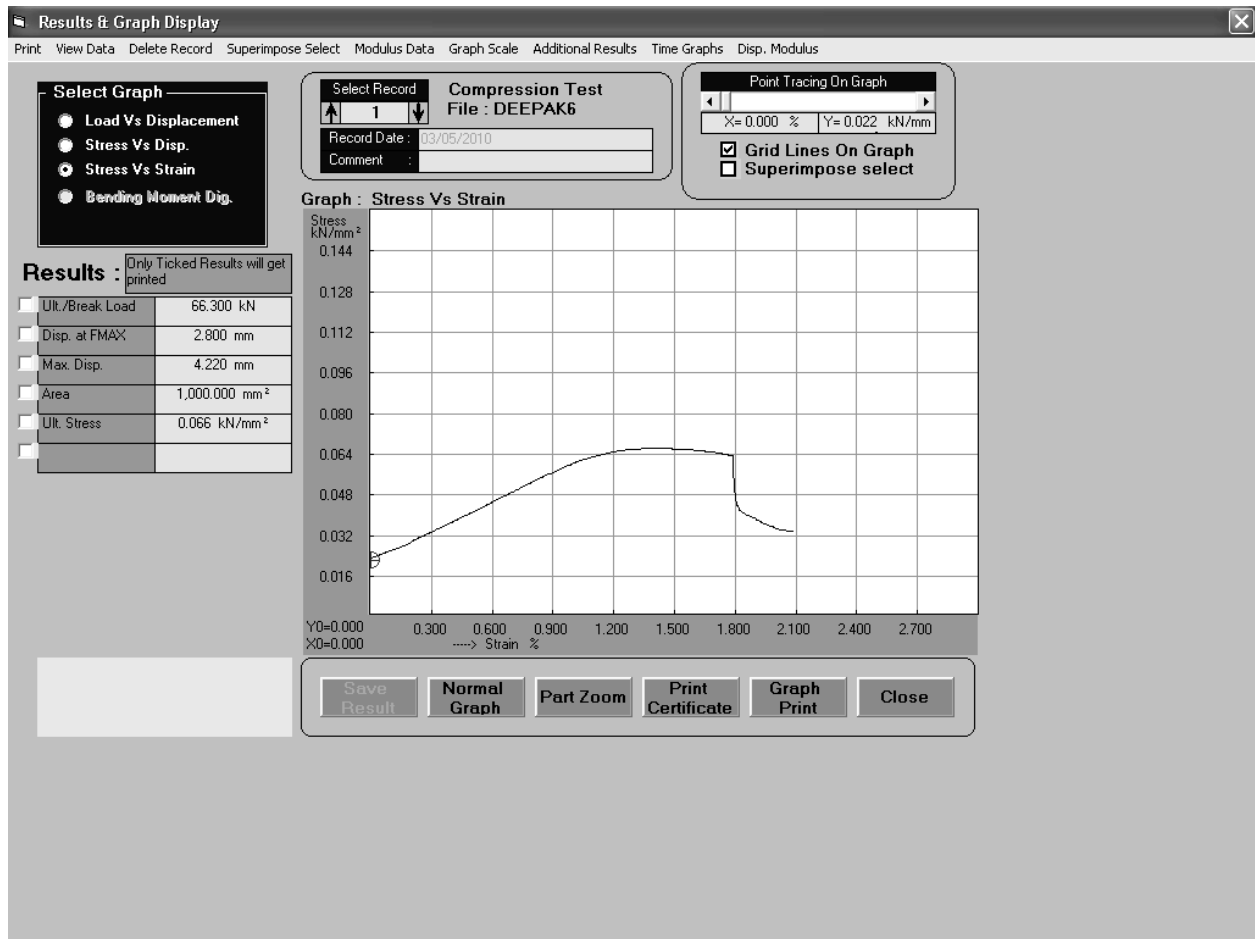
(graph-4-load vs. displacement of sample5)



*(graph-5-stress vs strain of sample5)*



(Graph-6-load vs displacement of sample6)



(Graph-7-stress vs strain of sample6)



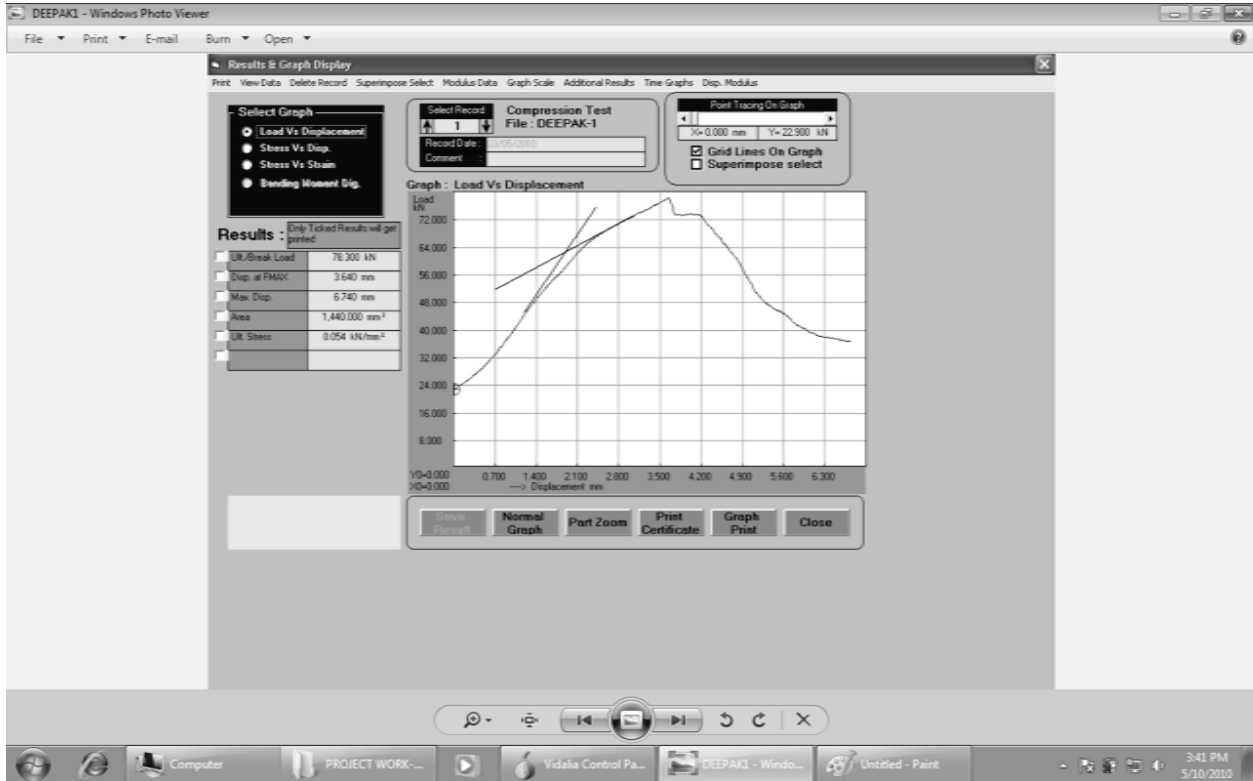
# *Chapter-4*

*Conclusion*

## *Aluminium plates:*

*According to the theoretical results the buckling load comes to be around 9.5kn and experimentally it is around 14.5kn. so a error of around 34% was obtained.*

## *Composite plates:*



(graph-8)

*Considering the buckling load of sample-1 we obtain a value around 62 kn and theoretically it is around 72.9 kn. But the moisture treatment of composite plates reduces their buckling strength and stiffness due to plasticization of polymer by absorbed moisture. Hence the results are adequate.*

# *Chapter-5*

*References*

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