FEM Analysis on Circular Stiffened plates using ANSYS

A Thesis Submitted to

National Institute of Technology, Rourkela

In Partial fulfillment of the requirement for the degree of

Bachelor of Technology

in

Mechanical Engineering

By

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Under the guidance of

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CERTIFICATE

This is to certify that the thesis entitled "**FEM Analysis of Circular Stiffened plates using ANSYS**"

submitted to the National Institute of Technology, Rourkela (Deemed University) by

Biswa Prakash Sukla, Roll No. **109ME0424** for the award of the Degree of **Bachelor of**

Technology in Mechanical Engineering is a record of bonafide research work carried out by him

under my supervision and guidance. The results presented in this thesis has not been, to the best of

my knowledge, submitted to any other University or Institute for the award of any degree or diploma.

The thesis, in my opinion, has reached the standards fulfilling the requirement for the award of the

degree of **Bachelor of technology** in accordance with regulations of the Institute.

Supervisor

Prof. ANIRBAN MITRA

ACKNOWLEDGEMENT

It is a great pleasure to express my gratitude and indebtedness to my supervisor **Prof. Anirban Mitra** for his guidance, encouragement, moral support and affection through the course of my work.

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Last but not the least I would like to extend my heartful gratitude to all other faculty members of Department of Mechanical Engineering, NIT Rourkela for their valuable advises and constant support at every stage of the completion of the project.

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ABSTRACT

In the present world, the increasing demand of structurally efficient and significantly higher strength to weight ratio structures is mostly served by Stiffened plates. These structural elements can be defined as plates reinforced by a single or a set of beams or ribs on one or both sides of the plate. So, stiffened plates are made up of plate elements, to which generally loading is applied, and beam elements located at discrete spacings in one or both directions. The present work deals with the structural behavior of a stiffened plate under static uniform loads. Firstly, we will consider a geometrically nonlinear beam problem by analyzing the large deflections of a beam of linear elastic material, under the action of transverse load along its length. Under the action of these external loads, the beam deflects into a curve called the elastic curve. Firstly, the relationship between the beam deflection and the loads would be established using Ansys and then the results would be extended to perform analysis on Stiffened plates. Stiffened plates can also be circular in shape with either radial or circumferential stiffeners. The present work aims to analyze a circular plate with radial stiffeners. The linear and nonlinear behavior of the beams would be studied under static and dynamic loading .The simulation analysis is completed with a numerical analysis of the system using the ANSYS program, a comprehensive finite element package, which enables students to solve the nonlinear differential equation. ANSYS provides a rich graphics capability that can be used to display results of analysis on a high-resolution graphics workstation.

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Chapter 1

INTRODUCTION

1.1 NEED FOR STIFFENED PLATES:

In the present world, the demand for structures with high stiffness is increasing day by day. One of the ways to deal with it is by using stiffeners. Countless mechanical structures are composed of stiffened plates. These structural elements can be defined as plates reinforced by a single or a set of beams or ribs on one or both sides of the plate. So, stiffened plates are made up of plate elements, to which generally loading is applied, and the beam elements are attached at discrete spacing in one or both directions. The material of the plate and stiffener can be identical or different. The main advantage of using stiffened plates is their significantly high stiffness to weight ratio compared to unstiffened plates[5]. Due to the increase in overall stiffness of the system, enhanced load carrying capacity and stability characteristics are obtained. So, it can be said that these are structurally efficient components that also have the added benefit of material savings and subsequent, economic and cost-effective design. Another advantage of stiffened plates is that they can be fabricated with ease and simplicity. Hence, it is no surprise that such structural components find wide-spread utilization in modern branches of civil, mechanical, structural and construction engineering. Stiffened plates are subjected to various types of loading conditions in their working environment. For instance, in case of bridge decks the stiffened plates are under lateral or transverse loads. On the other hand, longitudinal bending of the ship hull exerts longitudinal in-plane axial compression on the plates. The loading conditions on a component can be broadly classified into two classes, static (invariant with time) and dynamic loading (varies with time). Hence, the design of the plates must be carried out keeping in mind these two aspects of loading. Considerations for static design include desired load carrying capacities and deformations within prescribed limits, while, design based on dynamic considerations deals with mechanical behavior with respect to time varying excitations.

Applications of Stiffened Plates:

1. In aerospace and marine constructions, where minimization of weight of the components is of paramount interest, stiffened plates find extensive application.

2. They are used in off-shore constructions like oil rigs, marine constructions such as ship and submarine hulls, decks and bridges of ships.

3. In aerospace applications, aircraft wings are made out of stiffened plates. Apart from that they are also utilized in making advanced rocket launching structures.

4. Stiffened plates are of common occurrence in the field of highway bridges and elevated roadways, where they are generally employed to build the bridge decks.

5. Among land based structures, lock gates, box girders, plate girders etc. are also some of the fields of application for such plates.

6. In some building structures floor slab systems are often made out of these components in order to avoid uncomfortable vibrations.

7. There are some examples of stiffened plates being used in railway wagons, cargo containers, goods vehicle sidewalls etc.

In fact, there are virtually innumerable engineering applications of these components, which only serve to underline their efficiency, as well as their importance.

1.2 AIM OF THE PRESENT WORK:

In the present world, the increasing demand of structurally efficient and significantly higher strength to weight ratio structures is mostly served by Stiffened plates. The present work deals with the structural behavior of a stiffened plate under static uniform loads. Firstly, we will consider a geometrically nonlinear beam problem by analyzing the large deflections of a beam of linear elastic material, under the action of transverse load along its length. Under external loads, the beam deflects into a curve that is called the elastic curve. Firstly, the relationship between the beam deflection and the loads would be established using Ansys and then the results would be extended to perform analysis on Stiffened plates. Stiffened plates can also be circular in shape with either radial or circumferential stiffeners. The present work aims to analyze a circular plate with radial stiffeners. The linear and nonlinear behavior of the beams would be studied under static loading .The simulation analysis is completed with a numerical analysis of the system using the ANSYS program which is a comprehensive finite element package that enables the students to solve the nonlinear differential equations. ANSYS provides a rich graphics capability that can be used to display results of analysis on a high-resolution graphics workstation.

1.3 METHODOLOGY:

The analysis is done using Finite Element Method and the simulation is done using ANSYS. The advantage of using the FEM methodology is that unlimited number of stiffeners can be added to the model, which can be placed at any direction inside the plate element. The formulation accepts eccentric and concentric stiffeners of different cross-sections.

Finite Element Method:

The **finite element method (FEM)** (its practical application often known as **finite element analysis** (FEA) is a numerical technique for finding approximate solutions to partial differential equations (PDE) and their systems, as well as (less often) integral equations. In simple terms, FEM has an in built algorithm which divides very large problems (in terms of complexity) into small elements which can be solved in relation to each other. FEM solves the equations using the Galerkin method with polynomial approximation functions. The solution is obtained by eliminating the spatial derivatives from the partial differential equation. This approximates the PDE with

- a system of algebraic equations for steady state problems
- a system of ordinary differential equations for transient problems.

These equation systems are linear if the corresponding PDE is linear and vice versa. Algebraic equation systems are solved using numerical linear algebra methods. The ordinary differential equations that arise in transient problems are numerically integrated using techniques such as Euler's method or the Runge-Kutta method.

In solving PDE's, the major problem is to create an equation that approximates the equation to be analyzed, but is numerically stable, meaning that errors in the input and intermediate

calculations do not accumulate and cause the resulting output to be meaningless. There are many ways of doing this, which have their respective pros and cons. The finite element method is considered to be the best way for solving PDE's over complicated domains (like cars and oil pipelines), but when the domain changes for example in a moving boundary solid state reaction when the desired precision varies over the entire domain, or when the solution is not smooth. For example in a frontal car crash simulation where we need more accurate results in the front of the car and hence we can reduce the simulation cost in the rear end. Another instance is in weather prediction (which is done numerically), where it is more important to have accurate predictions over highly developing nonlinear phenomena (unpredictable natural calamities which happen, like cyclones) rather than relatively calm environment.

Geometric Non-Linearity:

Structures whose stiffness is dependent on the displacement which they may undergo are termed geometrically nonlinear. Geometric nonlinearity is responsible for stiffening of a loaded clamped plate, and buckling behavior in slender structures and components etc. It is necessary to take these effects into account for the computer simulation to predict the behavior accurately.

Material Non-Linearity:

Material Nonlinearity refers to the ability for a material to exhibit a nonlinear stress-strain (constitutive) response. Elasto-plastic, hyper-elastic, crushing, and cracking are good examples. Material non-linearity can also include temperature and time-dependent effects such as visco-elasticity or visco-plasticity. Material nonlinearity occurs due to some form of internal decomposition, characterized by a gradual weakening of the structural response as an increasing force is applied.

The analysis is done in a numerical way by the ANSYS program, a finite element package, which enables us to solve the linear and the nonlinear PDE's and thus the modulus of elasticity of the beam material is obtained . ANSYS is modeling and analysis software which helps in the modeling and analysis of required models, a FEM tool. It is used to analyze complex problems in mechanical structures, thermal processes, electrical fields, magnetics, and computational fluid dynamics. ANSYS provides a rich graphics environment, which is used to display results of analysis that re performed.

1.4 BEHAVIOUR OF CANTILEVER BEAM UNDER UNIFORM LOADING:

Beams are common elements of many architectural, civil and mechanical engineering structures and the study of the bending of straight beams forms an important and essential part of the study of the broad field of mechanics of materials and structural mechanics. All undergraduate courses on these topics include the analysis of the bending of beams, but only small deflections of the beam are usually considered. In such as case, the differential equation that governs the behavior of the beam is linear and can be easily solved. But as the load increases non-linearity comes into play. This can be demonstrated using a very simple experiment i.e. bending of a cantilever beam. The mathematical treatment of the equilibrium of this system does not involve great difficulty. Nevertheless, unless small deflections are considered, an analytical solution does not exist, since for large deflections a differential equation with a nonlinear term must be solved [7]. The problem is said to involve geometric nonlinearity. This type of nonlinearity is related to the nonlinear behavior of deformable bodies, such as beams, plates and shells, when the relationship between the extensional strains and shear strains, on the one hand, and the displacement, on the other, is taken to be nonlinear, resulting in nonlinear strain-displacement relationships.

Definition of static analysis:

A static analysis determines the effects of steady loading conditions on a structure, while ignoring inertia and damping effects, such as those caused by time varying loads.

A static analysis contains steady inertia loads, and time varying loads that can be assumed as static equivalent loads (such as static equivalent wind).

Static analysis is used to calculate the stresses, displacements, strains, and forces in structures caused by loads that do not contain inertia and damping effects. We assume that in steady loading the loads and the structure's response vary slowly with respect to time.

Various types of loading that can be applied in a static analysis are:

- Externally applied forces and pressure.
- Steady-state inertial forces (such as gravity).
- Nonzero displacements.
- Temperatures (for thermal strain).

Linear Vs. Nonlinear Analysis:

A static analysis can be either linear or nonlinear. We can allow all types of nonlinearities such as large deflections, plasticity, creep, stress stiffening, contact (gap) elements, hyper-elastic elements etc.

Information about nonlinear analysis

Ansys employs the "Newton-Raphson" approach to solve nonlinear problems. In this, the load is subdivided into a series of load increments. Load increments are applied in several load steps.

A nonlinear analysis is organized into three level of operations:

- The "top" level consists of the load steps that you define explicitly over a "time" span. Loads are assumed to vary linearly within load steps (for static analysis).

- Within each load step, you can direct the program to perform several solutions to apply the load gradually [6].

- At each sub step, the program will perform a number of equilibrium iterations to obtain a converged solution [6].

Chapter 2

LITERATURE SURVEY

Year	Author	Journal, Vol, Page	Theoretical/ Analytical/ Experimental/ Statistical	Software used	Method used	Material used	Findings
1999	Manoranjan Barik		Numerical and theoritical	C++	Newton-Raphson Iteration	ACM Element	Various classes of plates were analyzed and results correlated.
1997	G.J Tuvey, M. salehi	Vol. 63 No-4 pp.775-783	Numerical	Ansys	Dynamic Relaxation Algorithm	NA	
2011	Anirban Mitra, Prasanta Sahoo		Mathematical	FORTRAN	Energy methods	Aluminium	Dynamic behavior furnished in the form of back bone curves

Chapter 3

ANALYSIS

3.1 PROCEDURE FOR PERFORMING NON LINEAR ANALYSIS ON A CANTILEVER BEAM:

1. Go to Preferences->select structural

2. Then Pre-processor->Element Type ->Add/Edit->Select Solid tet 10 node 187 from the list of the elements

3. Material Properties ->Material Models -> select Structural-> linear ->elastic->isotropic-> values of EX and PRXY were given (71.7e09, 0.33 respectively).

4. Modeling ->Create -> Areas -> rectangular -> By dimensions

5. Modeling->Operate->extrude ->Areas->along Normal (required dimension was fed)

6. Meshing ->Mesh Tool (smart size and the shape of the mesh were chosen and then the structure was meshed)

7. Go to Solution ->analysis Type -> Sol'n Control-> and the following values were fed as shown in the figure 3.1
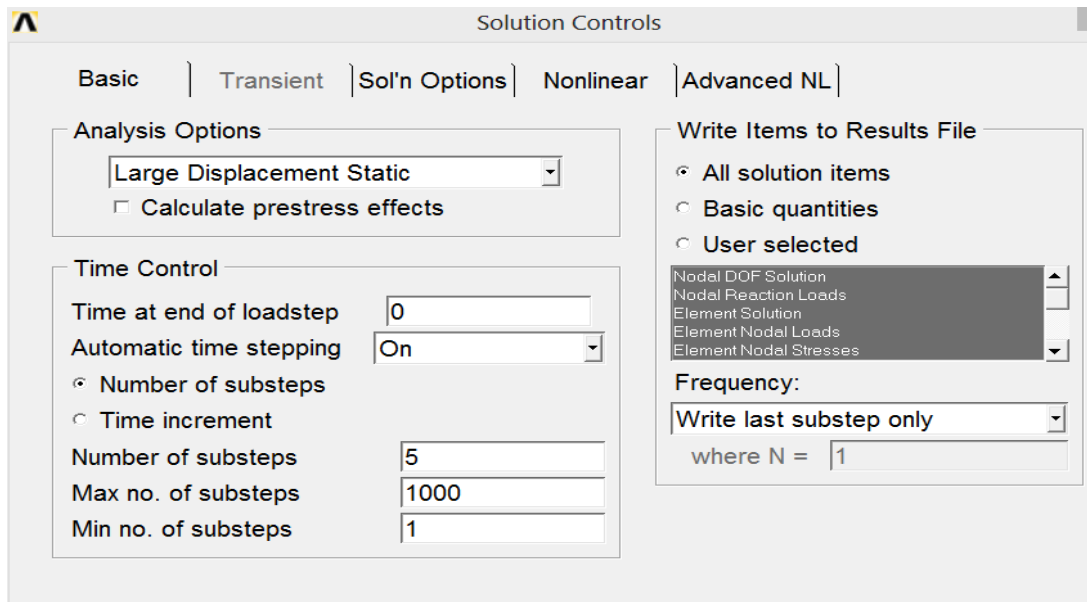
Figure 3.1 Values that are fed in Sol'n Control

8. Define Loads ->Structural-> Displacement ->On areas (the face which are to be fixed are selected and the displacement value is set to 0)

9. Define loads ->Structural->force/moment->On Nodes (where the required node is selected from the list of nodes)
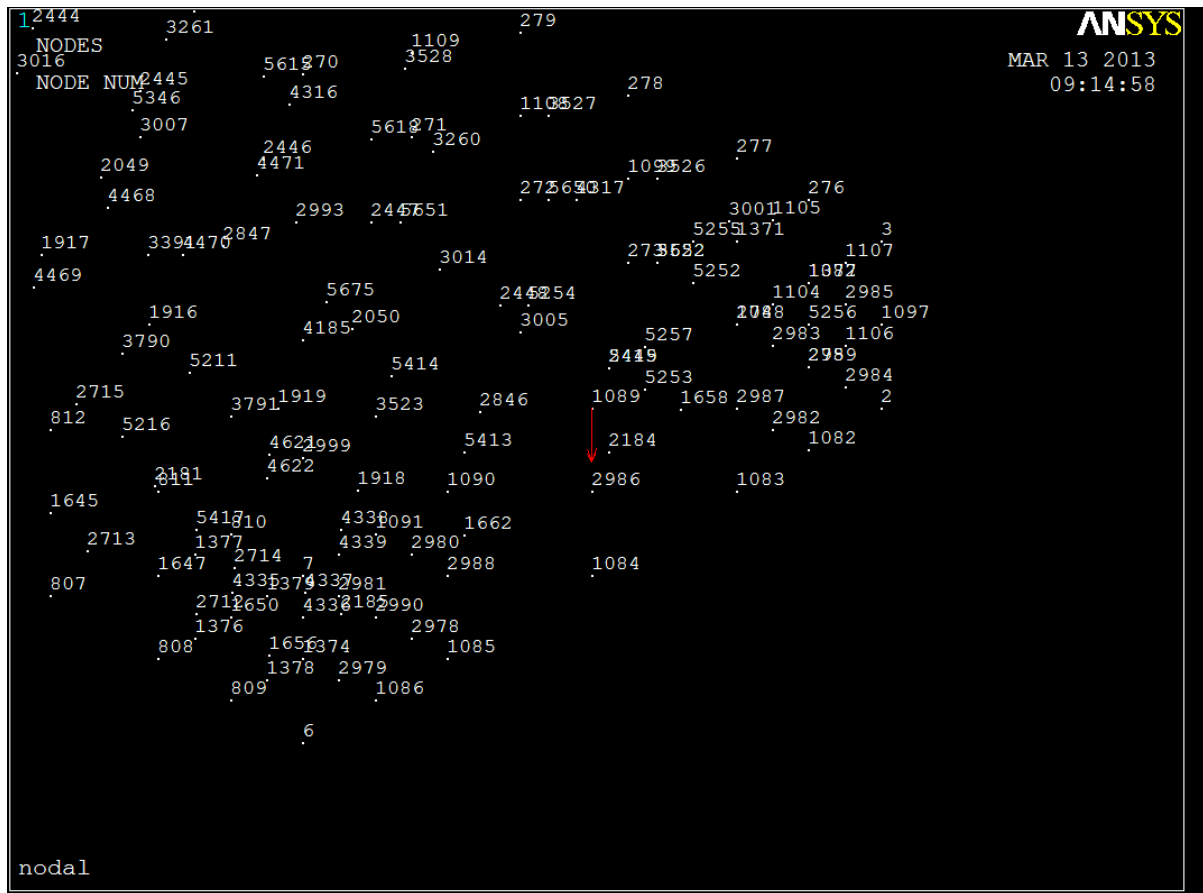
Fig 3.2 Nodal diagram of a cantilever beam

10. Solve ->Current LS

In order to obtain the deformed shape

Go to General Postproc ->Plot Results (select deformed shape)

3.2 PROCEDURE FOR PERFORMING NON LINEAR ANALYSIS ON A CANTILEVER BEAM (for Uniform Load):

1. Go to Preferences->select structural

2. Then Pre-processor->Element Type ->Add/Edit->Select Solid tet 10 node 187 from the list of the elements

3. Material Properties ->Material Models -> select Structural-> linear ->elastic->isotropic-> values of EX and PRXY were given(71.7e09, 0.3 respectively).

4. Modeling ->Create -> Areas -> rectangular -> By dimensions

5. Modeling->Operate->extrude ->Areas->along Normal (required dimension was fed)

6. Meshing ->Mesh Tool (smart size and the shape of the mesh were chosen and then the structure was meshed)

7. Go to Solution ->analysis Type -> Sol'n Control->and the following values were fed as shown in fig 3.1.
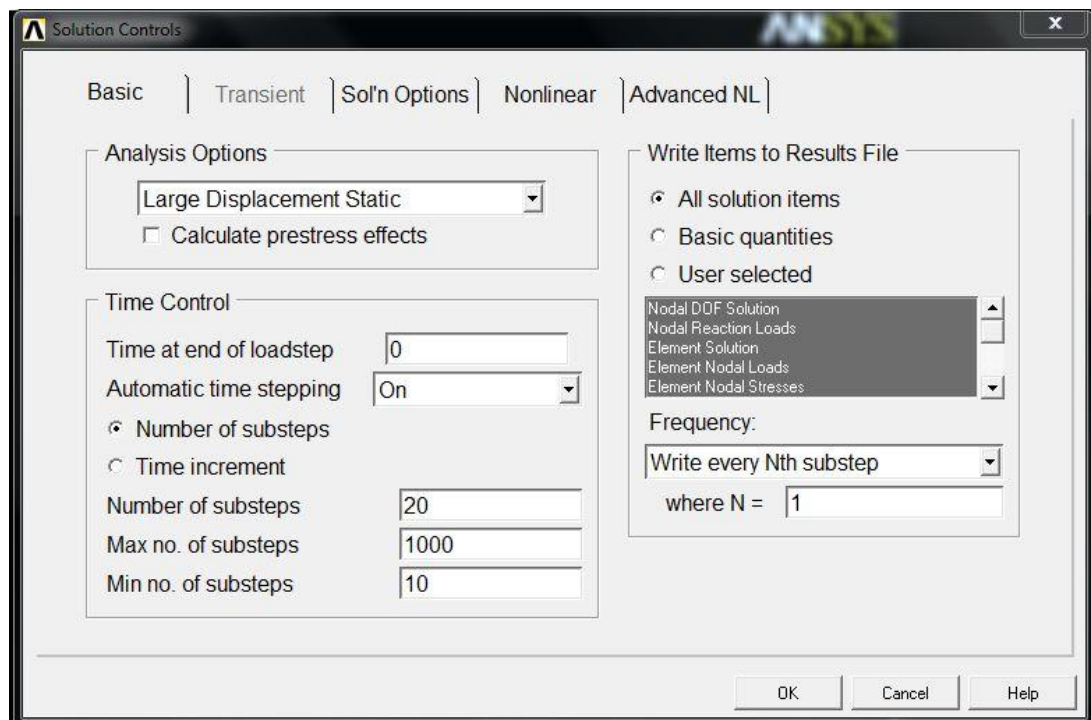
8. Define Loads ->Structural-> Displacement ->On areas (the face which are to be fixed are selected and the displacement value is set to 0)

9. Define loads ->Structural->Pressure->On Areas (where the required surface is selected).

10. Solve ->Current LS

In order to obtain the deformed shape

Go to General Postproc ->Plot Results (select deformed shape)

3.3 PROCEDURE FOR PERFORMING NON LINEAR ANALYSIS ON A CIRCULAR STIFFENED PLATE:

    A. **GEOMETRIC MODELLING**

    B. **NON LINEAR ANALYSIS ON CIRCULAR STIFFENED PLATES**

3.3.1 GEOMETRIC MODELLING:

1. Go to Preferences->select structural

2. Then Pre-processor->Element Type ->Add/Edit->Select Solid tet 10 node 187

3. Material Properties ->Material Models -> select Structural-> linear ->elastic->isotropic->

values of EX and PRXY were given (71.7e09, 0.3 respectively).

4. Modeling ->Create -> Areas-> Circle-> Annulus.

The center, inner and outer radius are entered in the pop up window.
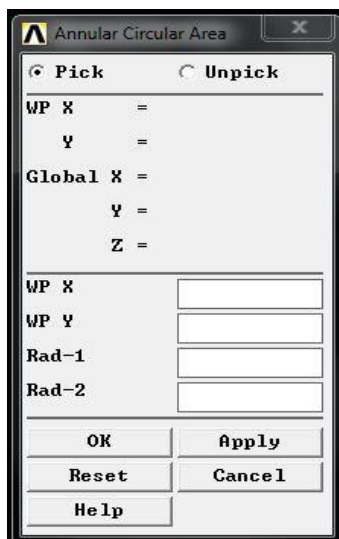
Fig 3.3 Selection of center and inner and outer radii

5. Modeling->Operate->extrude ->Areas->along Normal (required dimension is fed)

6. Then the stiffeners are added.

3.3.2 NON LINEAR ANALYSIS ON STIFFENED PLATES:

6. Meshing ->Mesh Tool (smart size nd the shape of the mesh were chosen and then the element was meshed)

7. Go to Solution ->analysis Type -> Sol'n Control->nd the following values were fed as

Figure 3.4 Values that are fed in Sol'n Control

8. Define Loads ->Structural-> Displacement -> On areas (the face which are to be fixed are selected and the displacement value is set to 0)

9. Define loads ->Structural->Pressure ->On Areas (where the required area is selected and the pressure value given).

10. Solve ->Current LS

11. General Postproc ->Plot Results (select deformed shape)

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Chapter 4

RESULTS AND DISCUSSIONS

RESULTS AND DISCUSSIONS:

4.1 VALIDATION :

Validation of the present method has been carried out by comparing the results available in literature. The results of the static analysis including the nonlinear results are validated with that of Manoranjan barik.

A clamped circular plate of diameter 25.4 mm. (1.0in.) is subjected to a uniform pressure of 6.8947 kPa (1.0psi). Initially the circular plate is unstiffened and then a stiffener along the diameter is added.

The central deflections of the circular plate and the stiffened circular plate are found to be $1.491*10^{-4}$ and $1.2039*10^{-4}$ respectively whereas those of Manoranjan Barik being $1.549*10^{-4}$ and $1.1496*10^{-4}$ respectively.

It is observed that the present results are in good agreement with the already established results.
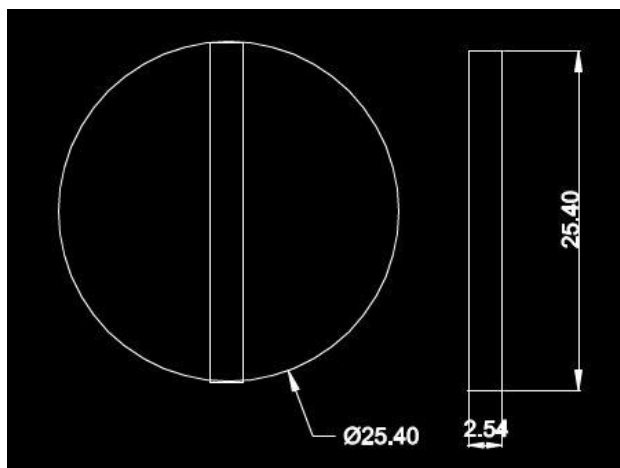
Figure 4.1 Diagram of the stiffened plate

4.2 BEHAVIOUR OF ANNULAR PLATES W.R.T. TO CHANGE IN INTERNAL DIAMETER:

The internal radius of the annular plate is varied keeping the outer radius constant and their respective results were studied.
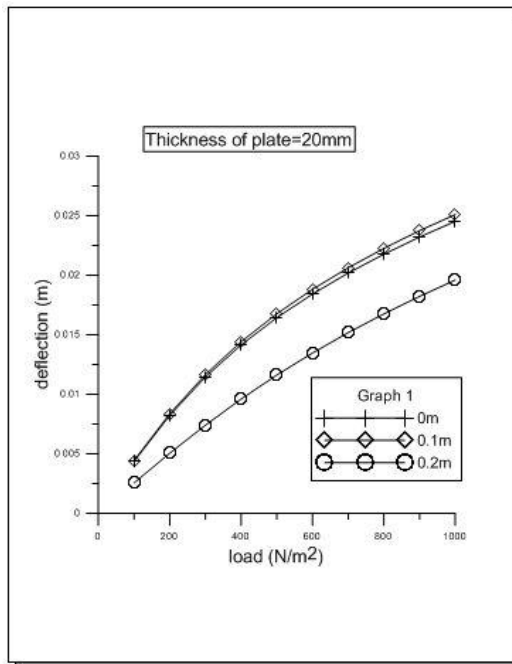
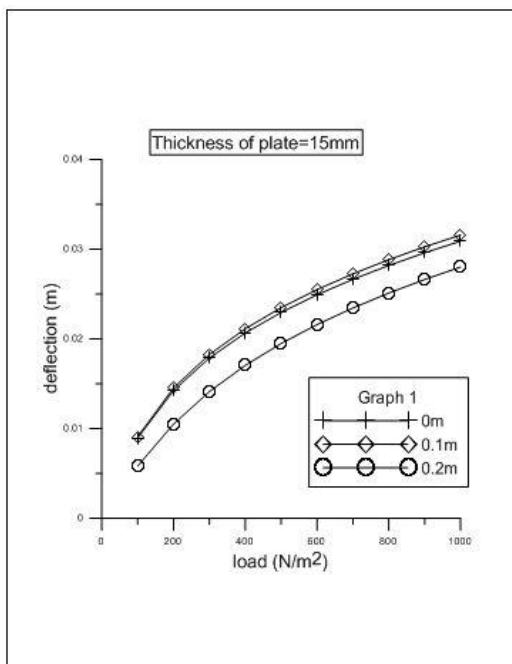Figure 4.2 Load vs deflection for 20mm plate
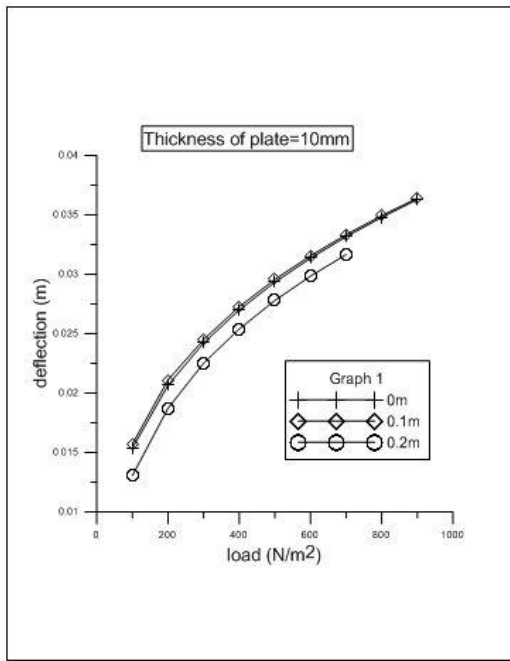

Figure 4.3 Load vs deflection for 15 mm plate

Figure 4.4 Load vs deflection for 10 mm plate

(a)LOAD VS MAXIMUM DEFLECTION:

From the above graphs it can be stated that the maximum deflection in the plate increases as the inner radius of the annular plate decreases. It is minimum when the inner radius is 20mm.

(b) DEFLECTION PROFILE:
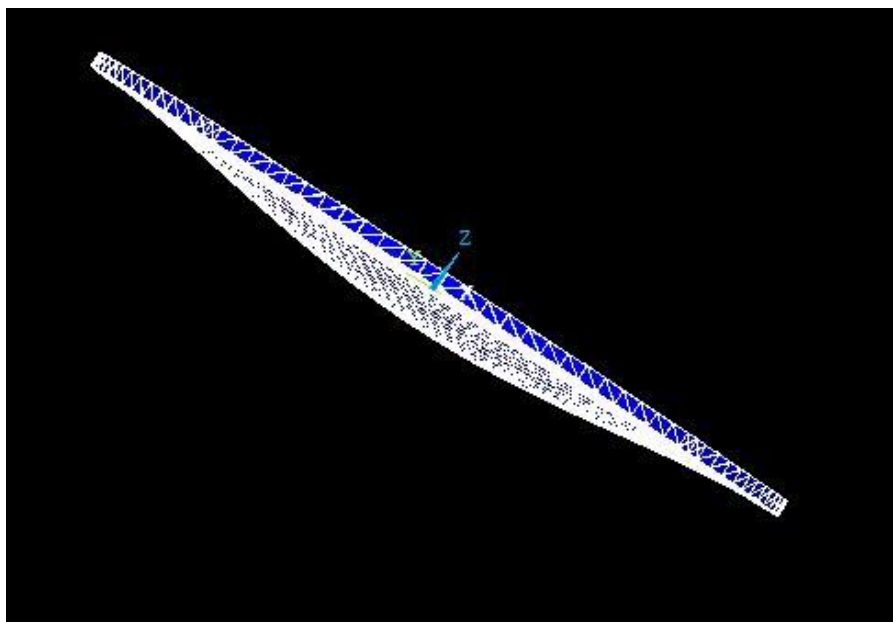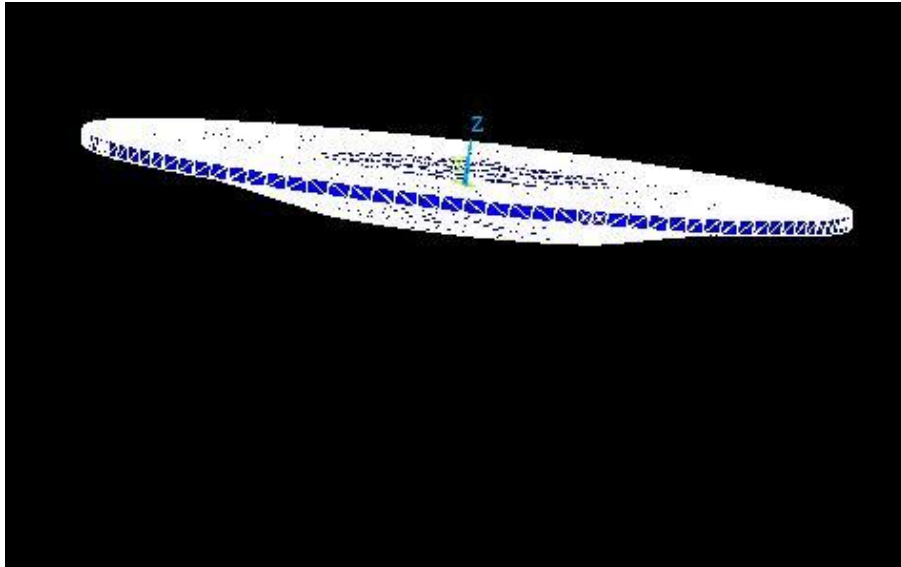

Figure 4.5 Deflection profile of the circular plate

Figure 4.6 Deflection profile of the annular plate

4.3 BEHAVIOUR OF CIRCULAR STIFFENED PLATES :

Stiffeners were added to the plates already analyzed and loads were applied to find out the deflections. First one stiffener was added along a diameter and then another stiffener was added perpendicular to the first stiffener and the analysis done.
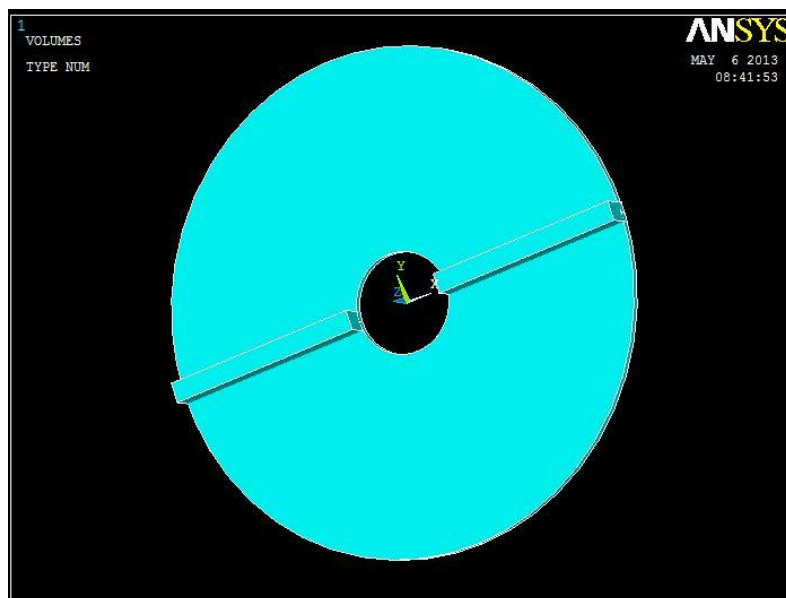

Figure 4.7 Geometry of annular plate with 0ne stiffener
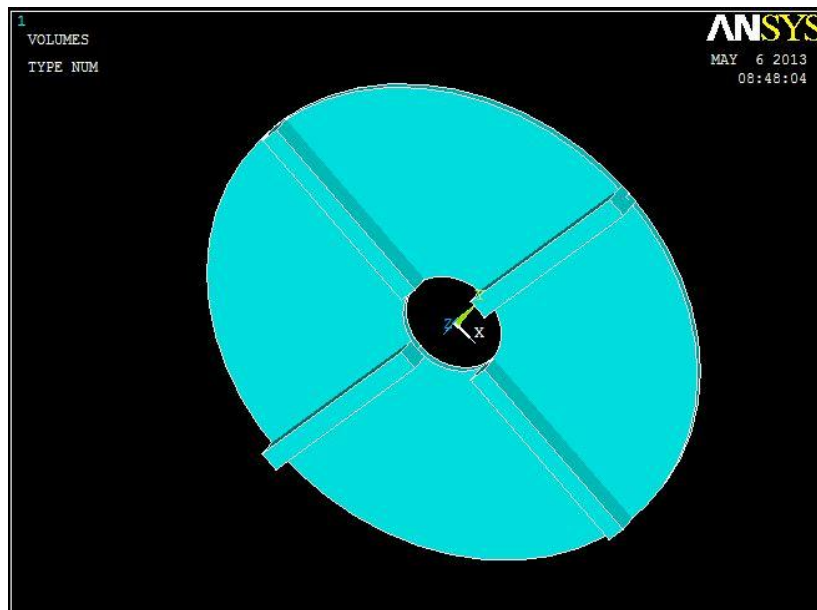
Figure 4.8 Geometry of annular plate with two stiffeners

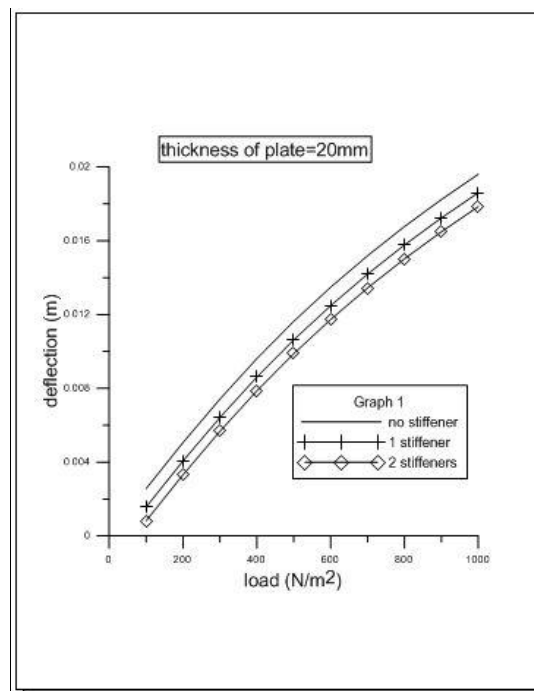Following graphs were plotted.

Figure 4.9 Load vs. deflection of annular plates of thickness 20mm with stiffeners
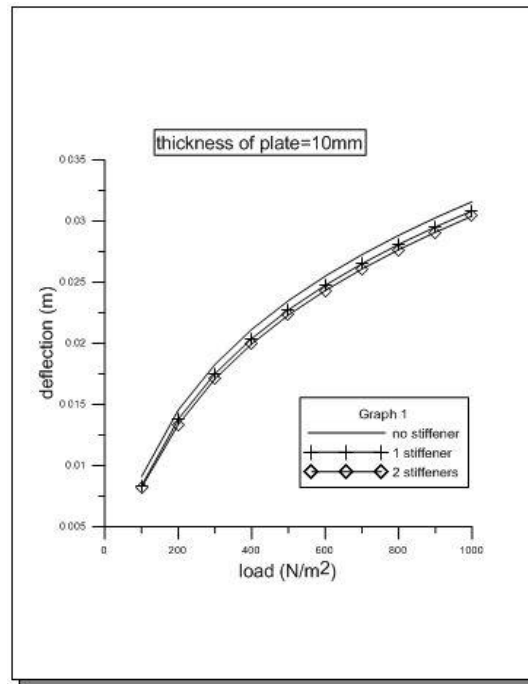
Figure 4.10 Load Vs. deflection of annular plates with thickness 10mm with stiffeners
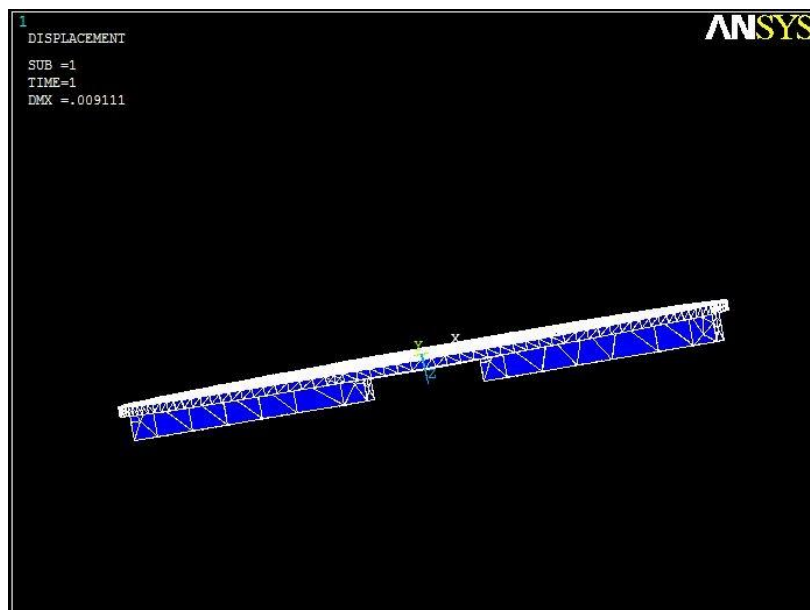

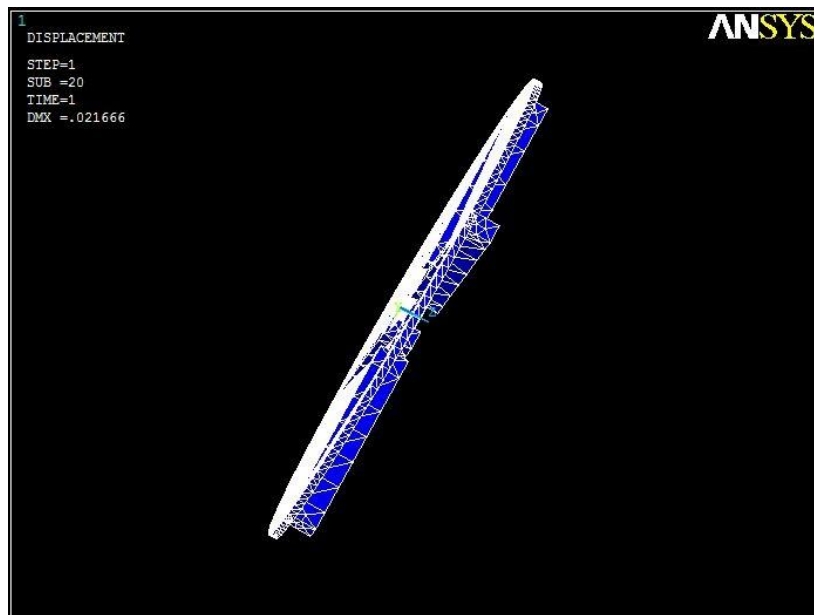Figure 4.11 Deflection profile of plate with one stiffener

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Figure 4.12 Deflection profile of plate with two stiffeners

Chapter 5

CONCLUSION

Conclusion :

1. The Results exhibit hardening type nonlinearity. Stiffness of the system increases with deflection. It shows the effect of stretching of mid-plane of the plate (geometric nonlinearity).

2. From the discussions regarding the thickness of plates, it can be safely said that the stiffness of the plates increases as the thickness increases.

3. Maximum deflection in the plate increases as the inner radius of the annular plate decreases.

4. Addition of stiffeners to the plates increased their load bearing capacity more so in case addition of two stiffeners than in the case of addition of one stiffener.

Chapter 6

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